

Tanta University	3 rd year, Computers & Control Dept.
Faculty of Engineering	Digital Control

Sheet 5

1. For the following open-loop Transfer functions:

$$i. \quad \overline{GH}(z) = \frac{0.0952kz}{(z-1)(z-0.965)}$$

$$ii. \quad \overline{GH}(z) = \frac{z+0.9}{z(z-0.5)}$$

$$iii. \quad \overline{GH}(z) = \frac{z+1}{(1-z)^2}$$

$$iv. \quad \overline{GH}(z) = \frac{z}{(z^2-1)(z^2-z+0.5)}$$

Calculate the steady-state error for input:

- a) A unit step
- b) A unit ramp
- c) $r(t) = 3u(t) + 2t$

2. For the following open-loop Transfer functions:

$$i. \quad \overline{GH}(z) = \frac{0.0952kz}{(z-1)(z-0.905)}$$

$$ii. \quad \overline{GH}(z) = \frac{k(z+0.9)}{(z-1)(z-0.7)}$$

$$iii. \quad \overline{GH}(z) = \frac{kz(z-0.5)}{(z-1)(z-0.8)}$$

$$iv. \quad \overline{GH}(z) = \frac{k(z-0.2)}{(z-1)(z+0.6)^2}$$

$$v. \quad \overline{GH}(z) = \frac{0.15k(z+0.7453)}{z(z-1)(z-0.4119)}$$

- a) Draw the root locus
- b) Calculate the range of K for stability

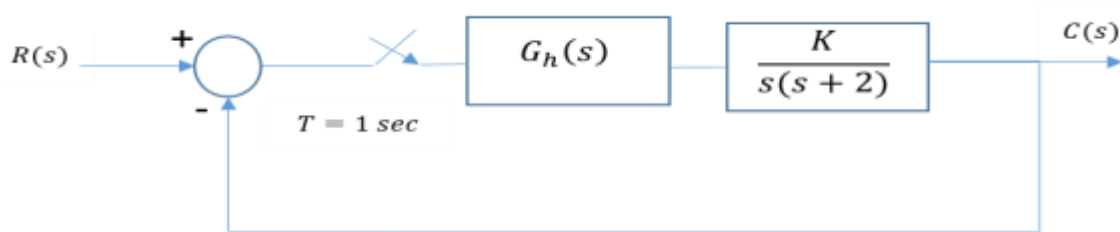
3. Consider the system given by:

$$\overline{GH}(z) = \frac{z + 1}{(1 - z)^2}$$

Assuming that the system is controlled by a gain controller (K) in a unity feedback:

- a) Plot the root locus
- b) Can you stabilize this system with a gain controller?

4. Find using the root locus technique the stability range for the system shown in figure below.



5. Assume a unity feedback system with the transfer function

$$G(z) = Tz^{-1}(1 - z^{-1})$$

And a proportional control gain K show that instability results if $KT > 0.5$.